The Fly America Act

All travel funded by United States federal government funds must be accomplished by U.S. Flag air carriers or U.S. code sharing to the extent that service by those carriers is available.

This means that the person travelling must fly a US carrier (code share is fine) if one is available. So the Turkish Airways flight from NY to Istanbul would not work, but the United/Lufthansa flight via Munich would work.